

Review

Friday, November 17, 2023 4:24 PM

HW 3 Ex. 6.5.7

Exercise 6.5.7 Use the fact that the period of $f_{7,247}$ is 12 to determine the factors of 247. ■

$$f(x) = 7^x \pmod{247} \implies r = 12$$

$$\text{GCD}((a^{\frac{r}{2}} + 1), N) \text{ and } \text{GCD}((a^{\frac{r}{2}} - 1), N)$$

$$\begin{aligned} & \text{gcd}(7^{12/2} + 1, 247) \\ &= \text{gcd}(117, 650, 247) \\ &= 13 \end{aligned}$$

$$\begin{aligned} & \text{gcd}(117 \cdot 649 - 1, 247) \\ &= 19 \end{aligned}$$

$$\begin{aligned} & 7^6 + 1 \pmod{247} \\ &= 78 \pmod{247} \\ 247 &= 3 \cdot 78 + 13 \leftarrow \\ 78 &= 6 \cdot 13 + 0 \end{aligned}$$

$$12 \times \frac{13}{2}$$

Exer 6.5.5

$$n = 8, \quad m = 16$$

Ex or 9.2.2

50% of the matched basis

$$\implies 25\% \text{ of } n.$$